



# *The Use of a Self-Evolving Additive Inflation in the CNMCA Ensemble Data Assimilation System*

*Lucio Torrisi and Francesca Marcucci  
CNMCA, Italian National Met Center*





# Outline

- Implementation of the LETKF at CNMCA-the Italian National Met Center
- Treatment of model error in the CNMCA-LETKF
  - The Self Evolving Additive Noise formulation
    - Forecast verification over 20-days test period
  - The SPPT (Stochastic physics perturbation tendencies) implementation
- Summary and future developments





# Ensemble Kalman Filter (LETKF) at the Italian Nat Met Center

- At CNMCA the **LETKF** (Hunt et al. 2007) formulation was chosen, because **algorithmically simple** to code, intrinsically parallel, etc.

- **OPERATIONAL SINCE JUNE 2011**

Analysis  
Ensemble Mean

$$\bar{x}^a \dagger \bar{x}^b \hat{G} X^b \bar{w}^a$$

Analysis  
Ensemble Perturb.

$$X^a \dagger X^b W^a$$

Analysis  
Ensemble

$$x^a \dagger x^b \hat{G} X^b w^a$$

$$\bar{w}^a \dagger \tilde{P}^a Y^{bT} R_1^{-1} (y - H(\bar{x}^b))$$

$$\tilde{P}^a \dagger [(m-1)I \hat{G} Y^{bT} R_1^{-1} Y^b]^{H1}$$

$$Y^b \dagger [(H(x_1^b) - \overline{H(x^b)}), \dots, (H(x_m^b) - \overline{H(x^b)})]$$

$$W^a \dagger [(m-1)\tilde{P}^a]$$

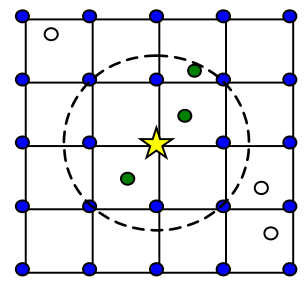
$$w^a \dagger W^a \hat{G} [\bar{w}^a, \dots, \bar{w}^a]$$

- 40+1 member ensemble at 0.09° (~10Km) grid spacing 45 vertical lev
- 6-hourly assimilation cycle run and (T,u,v,pseudo-RH,ps) as a set of control variables

Observations: RAOB (also 4D), PILOT, SYNOP, SHIP, BUOY, Wind Profilers, AMDAR-ACAR-AIREP, MSG3-MET7 AMV, MetopA-B/Oceansat2 scatt. winds, NOAA/MetopA-B AMSUA/MHS radiances

Horizontal/vertical localization (obs weight smoothly decay with a pseudo-gaussian function of distance)

Adaptive selection radius based on a fixed number of effective obs





# Treatment of model error

In the **operational CNMCA-LETKF** implementation, model errors and sampling errors are taken into account using:

- **Multiplicative Inflation: Relaxation to Prior Spread** according to Whitaker et al (2012)

$$\text{an. pert.} \quad \mathbf{x}'_a = \mathbf{x}'_a \sqrt{\alpha \frac{\sigma_b^2 - \sigma_a^2}{\sigma_a^2} + 1} \quad \alpha = 0.95$$

$\sigma^2 = \text{variance}$

- **Additive Noise from EPS** (climat. noise before june 2013)

$$\text{an. memb.} \quad \mathbf{x}_i^a \leftarrow \mathbf{x}_i^a + \alpha \mathbf{x}_i^n, \quad \alpha \mathbf{x}_i^n \sim N(0, \mathbf{Q}) \quad \alpha \text{ Scale factor}$$

$\mathbf{x}_i^n$  36-12h/42-18h forecast differences valid at analysis time

- **Lateral Boundary Condition Perturbation** of determ. IFS using EPS

- **Climatological Perturbed SST**

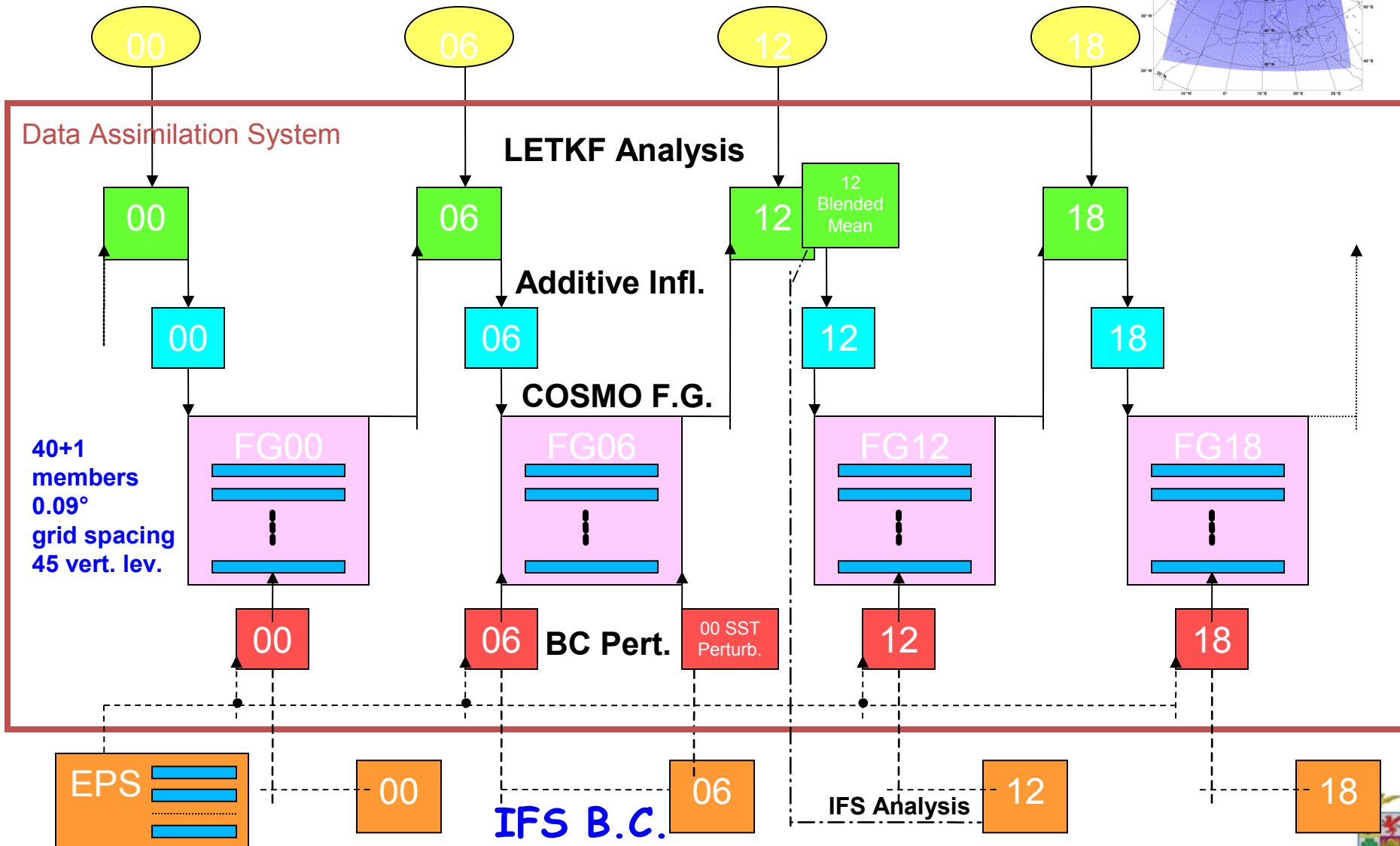
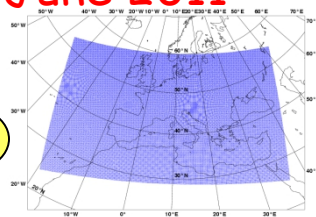




# CNMCA LETKF DA SYSTEM

Pre-operational from Dec 2010. Operational from 1 June 2011

## Observations ( $\pm 6h$ )



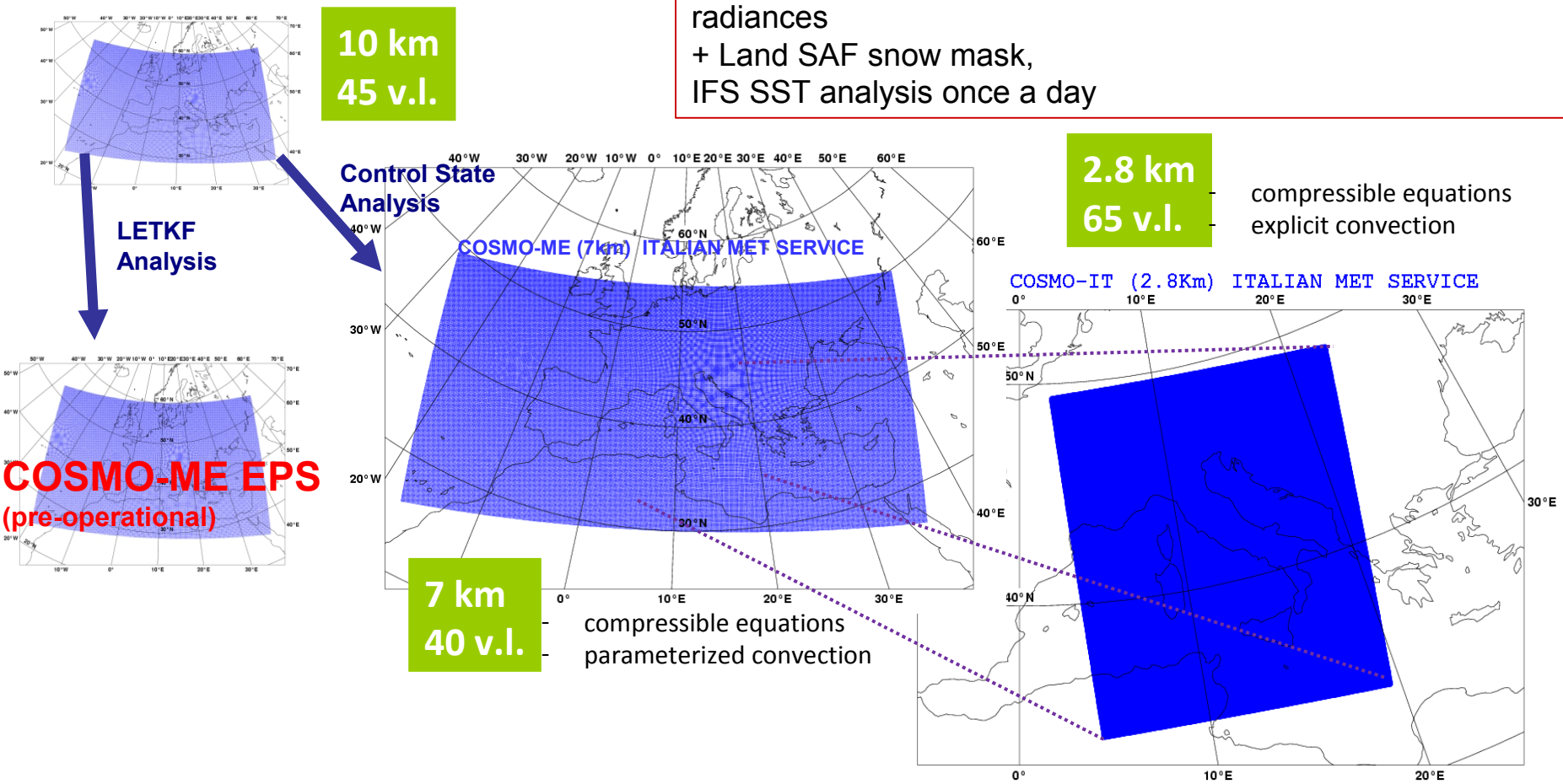




# CNMCA NWP SYSTEM since 1 June 11

LETKF analysis ensemble (40+1 members) every 6h using  
 RAOB (also 4D), PILOT, SYNOP, SHIP, BUOY, Wind  
 Profilers, AMDAR-ACAR-AIREP, MSG3-MET7 AMV, MetopA-  
 B/Oceansat2 scatt. winds, NOAA/MetopA-B AMSUA  
 radiances  
 + Land SAF snow mask,  
 IFS SST analysis once a day

## Ensemble Data Assimilation:





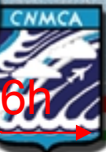
# Self-Evolving Additive Noise

**AIM: Find additive perturbations that are both consistent with model errors statistics and a flow-dependent noise**

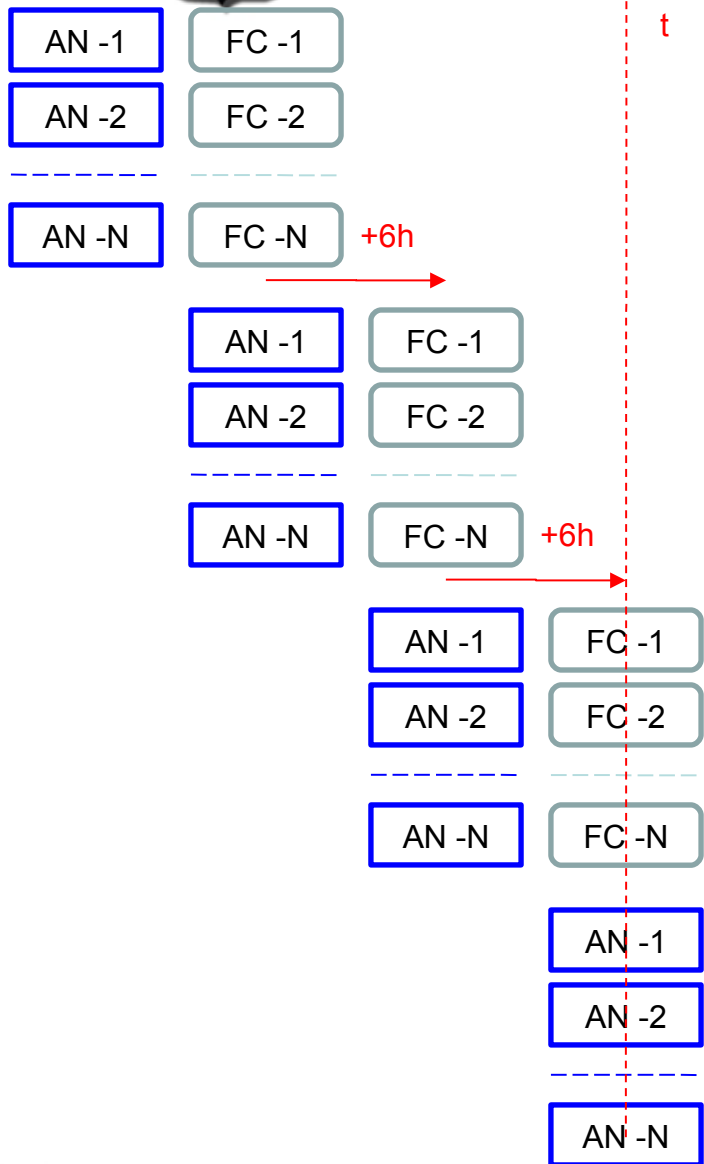
The self-evolving additive inflation (idea of Mats Hamrud – ECMWF) is chosen. The idea is different from that of the evolved additive noise of Hamill and Whitaker (2010)

- Difference between ensemble forecasts valid at the analysis time is calculated. The mean difference is subtracted to yield a set of perturbations that are scaled and used as additive noise. The ensemble forecasts are obtained by the same ensemble DA system extending the end of the model integration.
- The error introduced during the first hours may have a component that will project onto the growing forecast structures having probably a beneficial impact on spread growth and ensemble-mean error





# Self-Evolving Additive Noise



Additive noise valid at  $t$

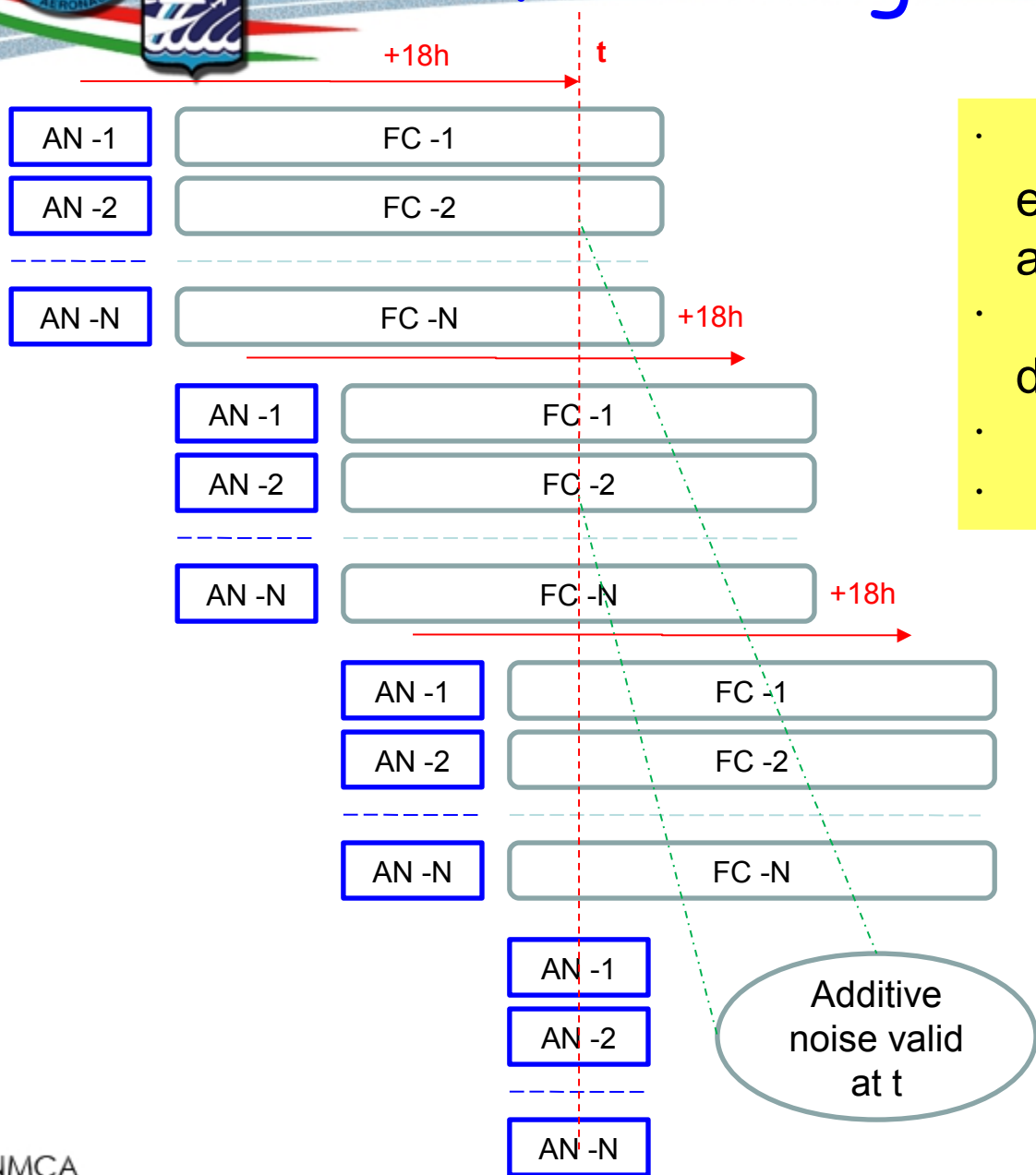
The end of model forecast  
Integration needs to be extended







# Self-Evolving Additive Noise



- Compute the difference of ensemble forecasts (i.e. 18h and 12h ) valid at time  $t$
- Remove the mean difference
- Scale the perturbations
- Add to the  $t$  analysis



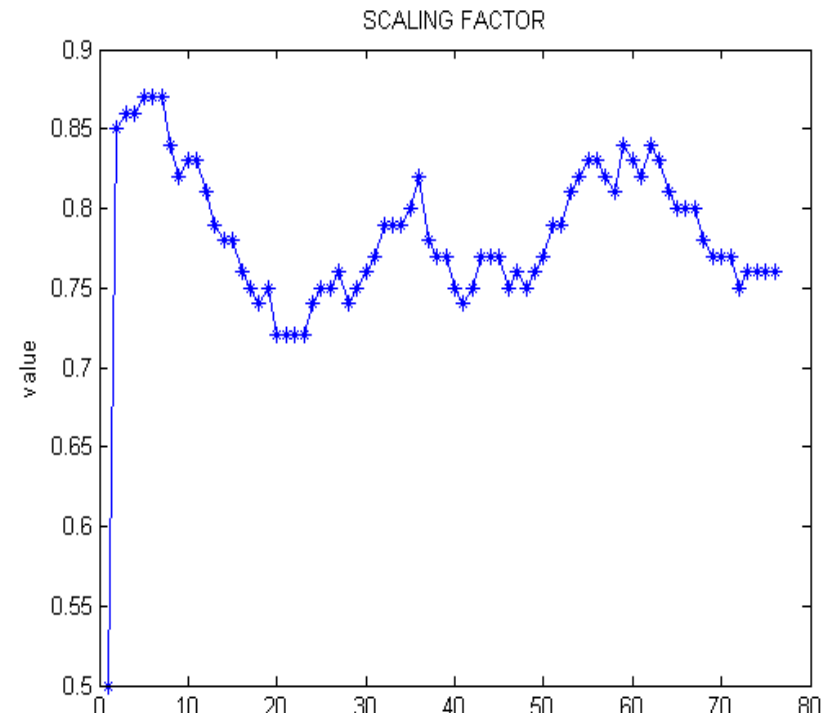
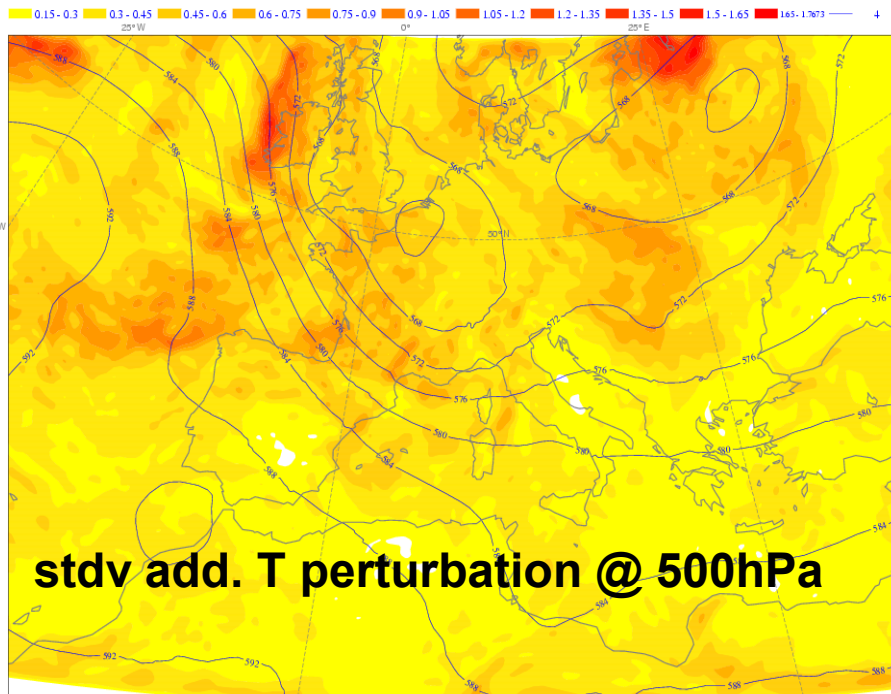


# Self-Evolving Additive Noise

Features of the first version:

$$\mathbf{X}_i^a \leftarrow \mathbf{X}_i^a + \alpha \mathbf{X}_i^n,$$

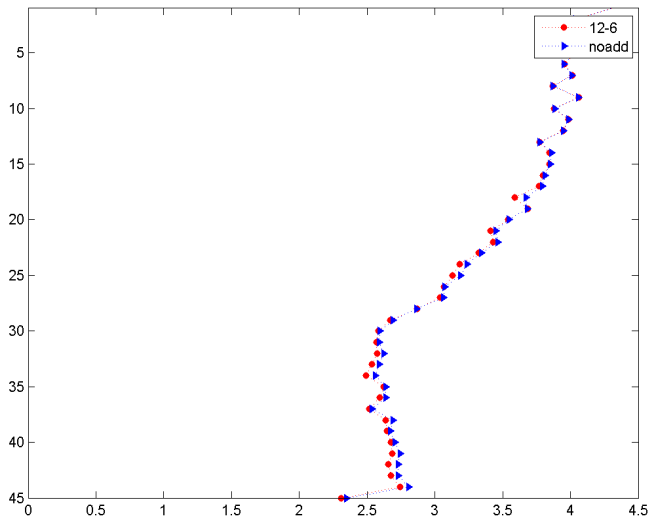
- 12h-6h forecast differences
- spatial filtering of ensemble difference using a low pass 10th order Raymond filter
- Adaptive scaling factor using the surface pressure obs inc statistics



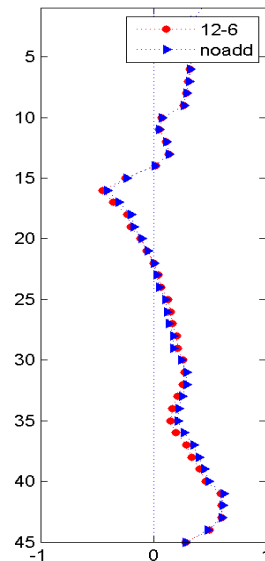


# Obs Increment Statistics

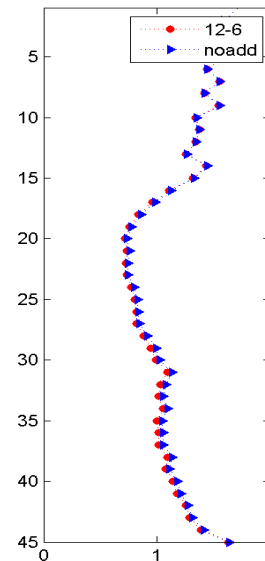
RMSE WIND VECTOR



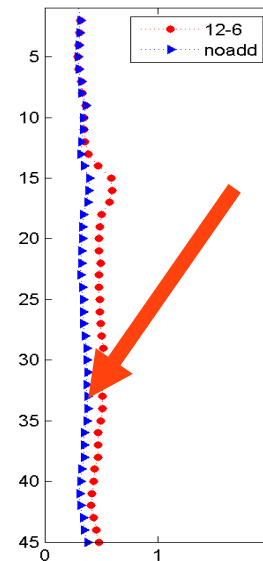
SCAD:ALL BIAS T



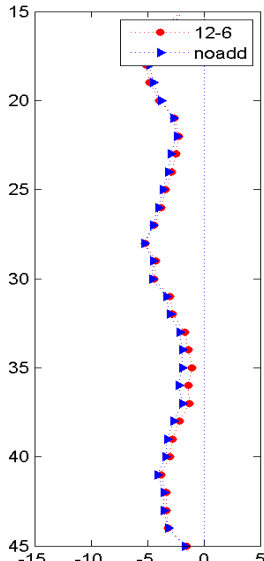
STDV T 1021 1110



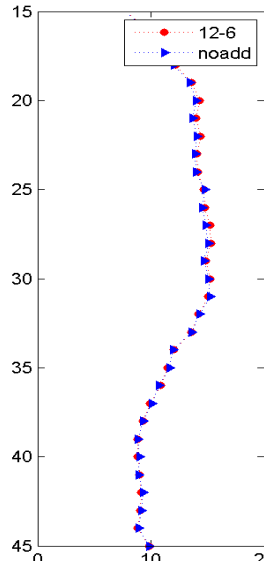
SPREAD T



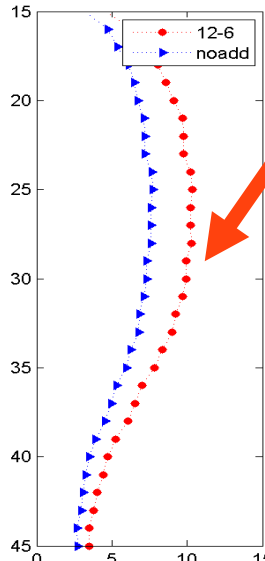
SCAD:ALL BIAS RH



STDV RH 1021 1110



SPREAD RH



OBS INCREMENT ON **MODEL**  
LEVELS (TEMP + RAOB obs)  
**NO ADDITIVE** VS **EVOLVED ADD**

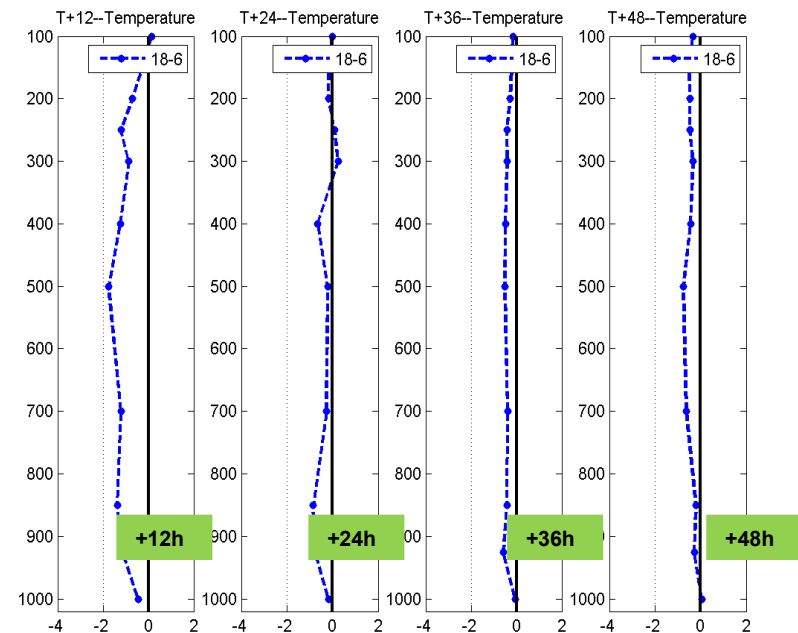
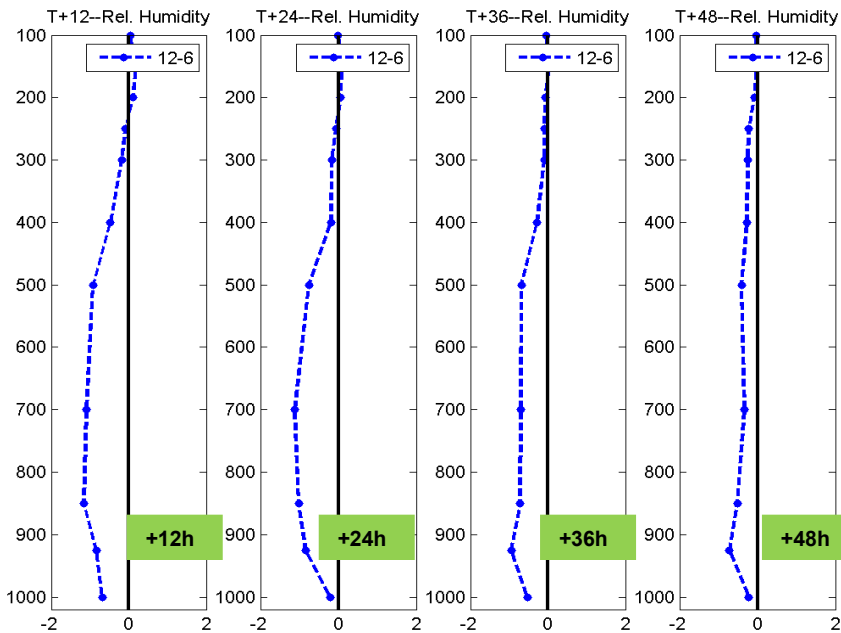
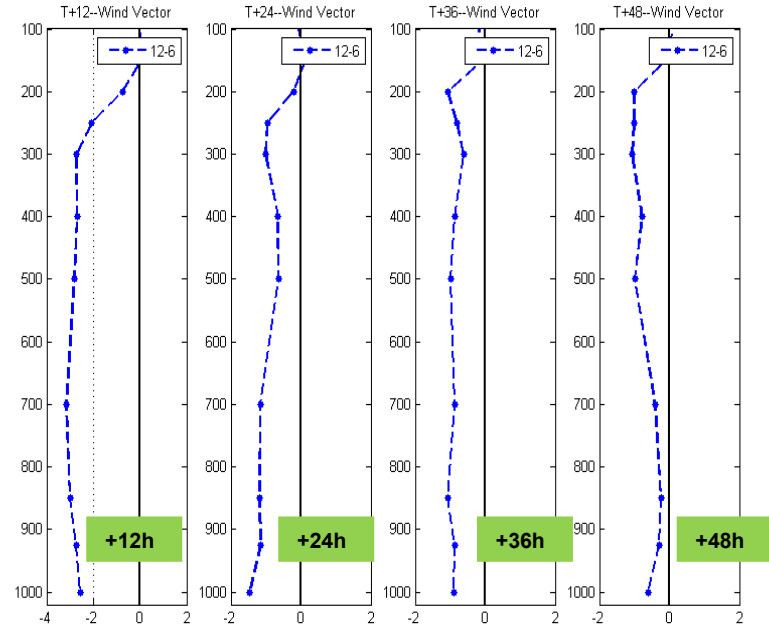
21 oct 2013 – 10 nov 2013





# Forecast Verification

Relative difference (%) in RMSE, computed against IFS analysis, with respect to **NO-ADDITIVE** run for 00 UTC COSMO runs from 21-oct 2013 to 10 nov 2013  
*negative value = positive impact*





# Self-Evolving Additive Noise

*Can we get some benefit increasing  
the time difference between  
forecasts ?*

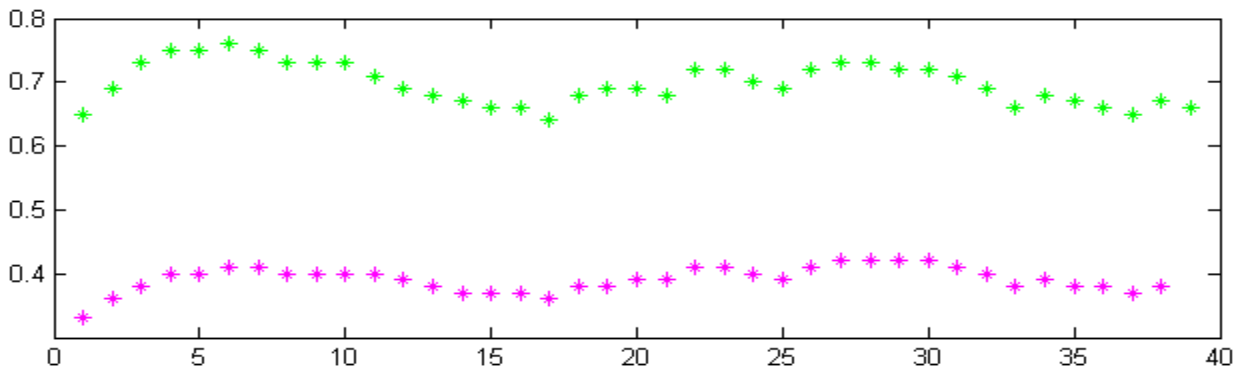
*18-6 h vs 12-6 h*







# Self-Evolving Additive Noise

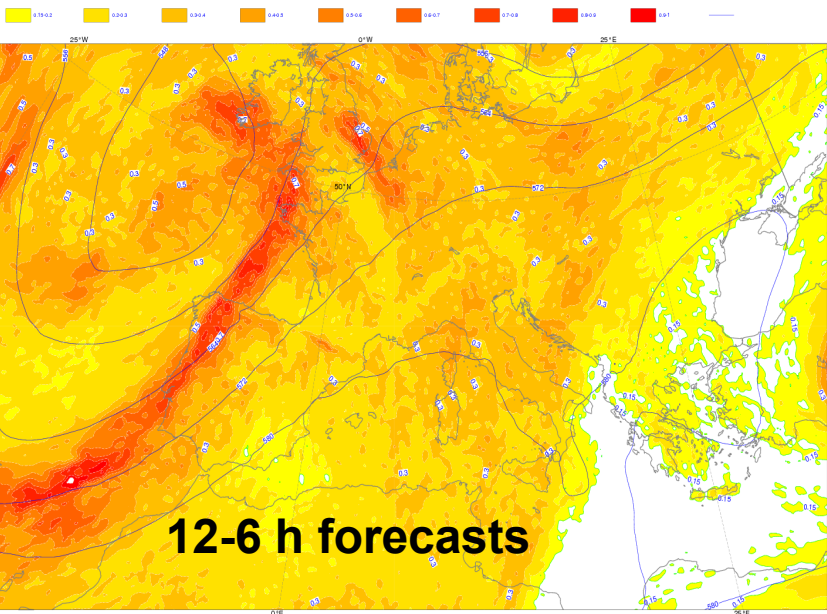


12-6 h forecasts

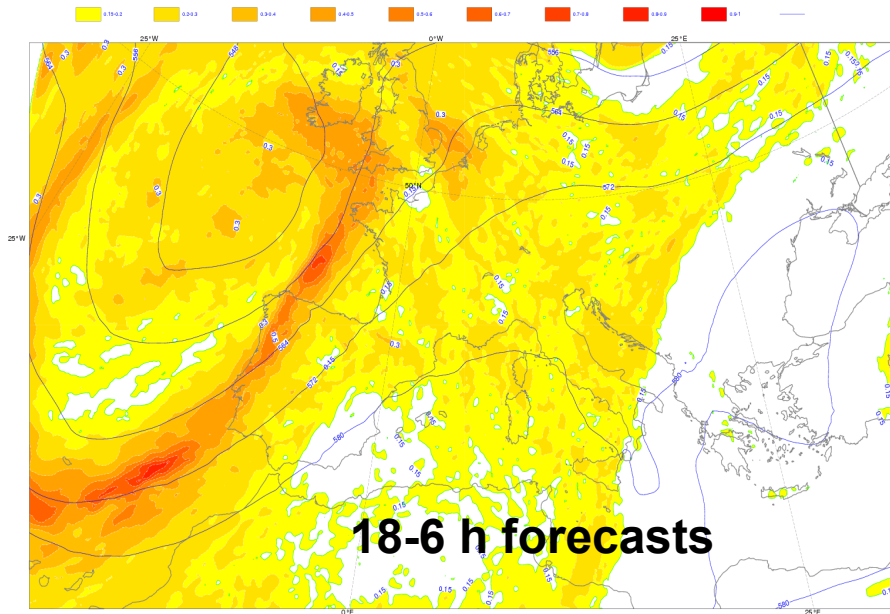
18-6 h forecasts

stdv add. T perturbation @ 500hPa

Friday 25 October 2013 00 UTC ecmf t+0 VT:Friday 25 October 2013 00 UTC 500 hPa\_Geopotential  
Friday 25 October 2013 00 UTC cmc t+0 VT:Friday 25 October 2013 00 UTC hybrid\_layer\_Temperature

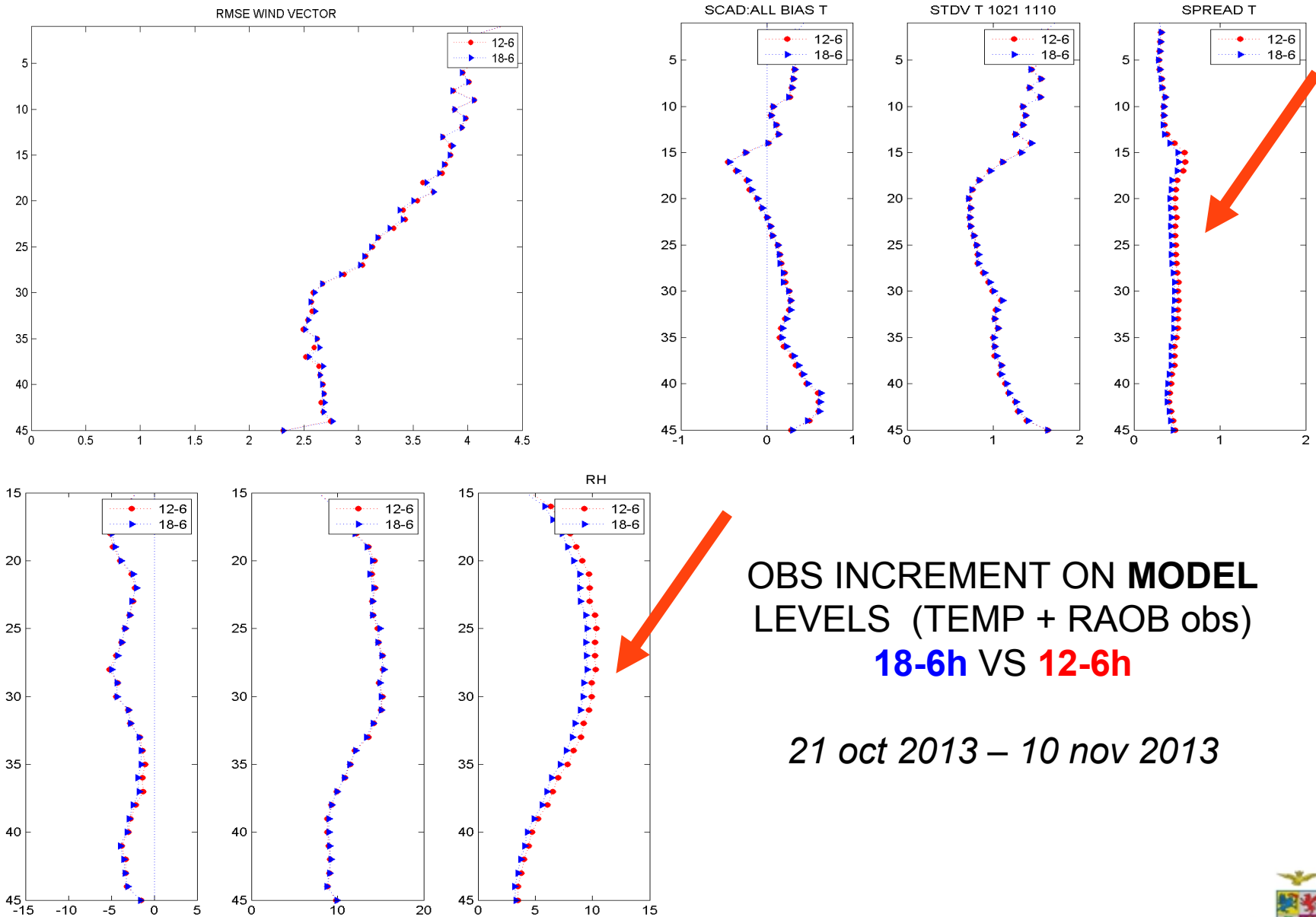


Friday 25 October 2013 00 UTC ecmf t+0 VT:Friday 25 October 2013 00 UTC 500 hPa\_Geopotential  
Friday 25 October 2013 00 UTC cmc t+0 VT:Friday 25 October 2013 00 UTC hybrid\_layer\_Temperature





# Obs Increment Statistics



OBS INCREMENT ON **MODEL**  
LEVELS (TEMP + RAOB obs)  
**18-6h** VS **12-6h**

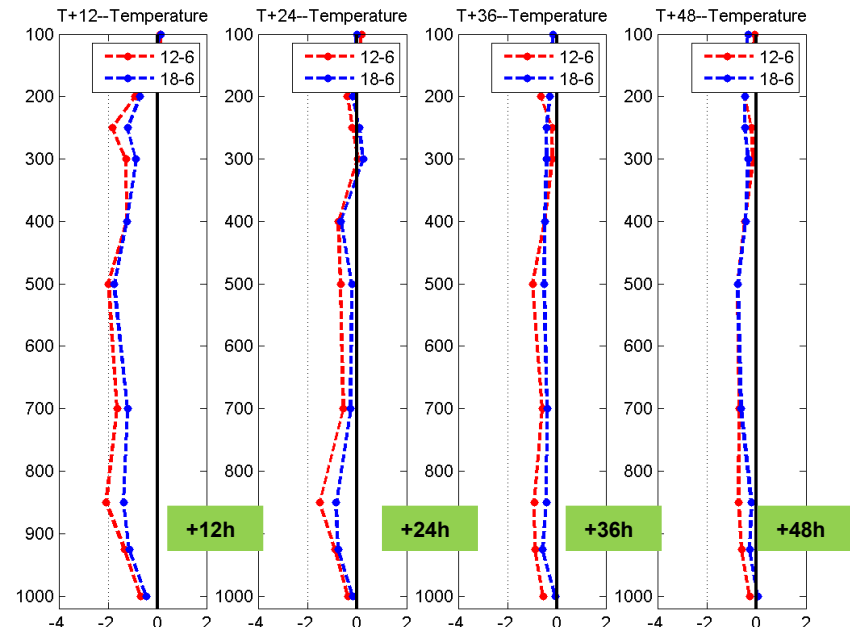
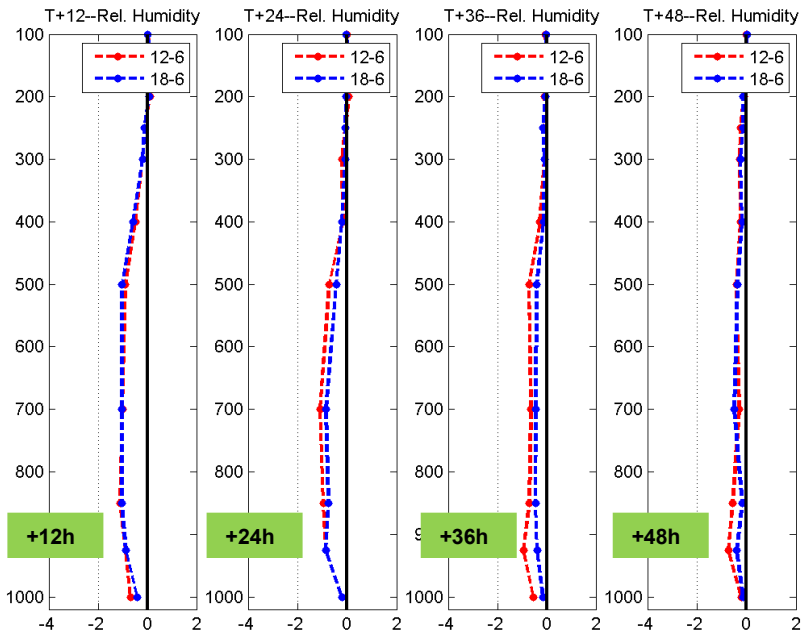
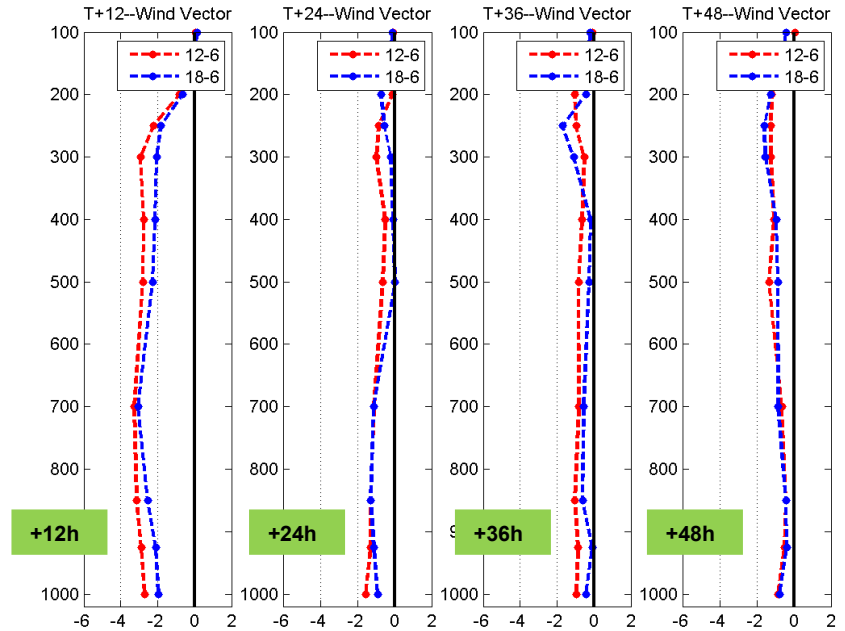
*21 oct 2013 – 10 nov 2013*





# Forecast verification

Relative difference (%) in RMSE, computed against IFS analysis, with respect to **NO-ADDITIVE** run for 00 UTC COSMO runs from 21-oct 2013 to 10 nov 2013  
*negative value = positive impact*





# Operational Additive Noise

On June 2013 (HRM → COSMO) a new additive inflation formulation was needed for the operational COSMO-LETKF since:

- The previous version of CNMCA-LETKF used a climatological additive noise based on HRM model.
- A climatological forecast database for COSMO at 0.09° and 45 v.l. is not available on the current integration domain
- Climatological additive inflation has the technical disadvantage to require an “enough” long period of 36/48h forecasts (need to re-run the model or to interpolate old runs to the new resolution)

Moreover:

- A deficiency of climatological additive perturbations is that they are not dynamically conditioned to project onto the growing forecast structures (no relevance of flow of the day). It may take a while to project strongly.







# Additive Noise from IFS

## First (!not last) solution:

- The difference between EPS ensemble forecasts valid at the analysis time is computed and interpolated on the COSMO grid (36h and 12h at 00/12UTC run and 42h and 18h at 06/18UTC run)
- EPS forecasts on pressure levels are currently used.
- The mean difference is removed to yield a set of perturbations that are globally scaled and used as additive noise.

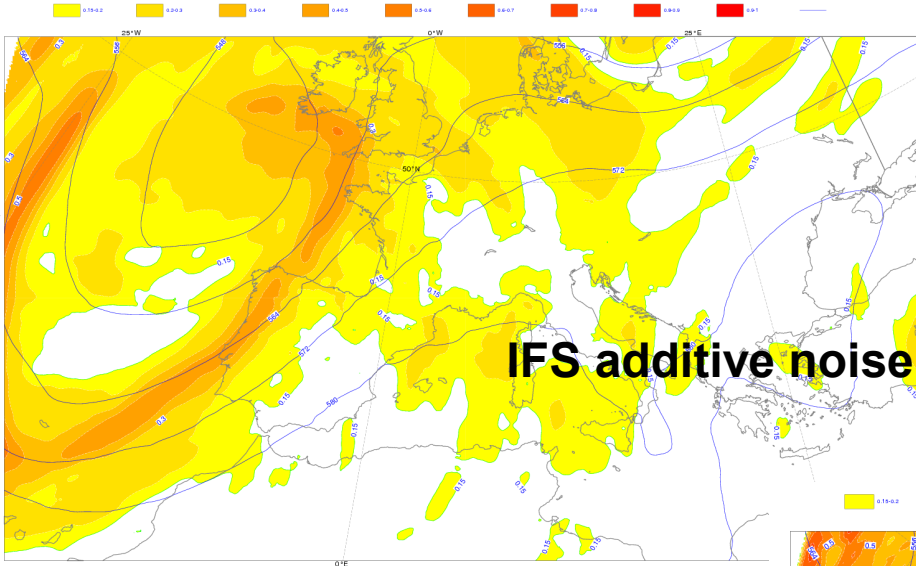
This additive noise, derived from IFS model, is not consistent with COSMO model errors statistics, but it may temporarily substitute the climatological one (avoiding a decrease of the spread in the CNMCA COSMO-LETKF).



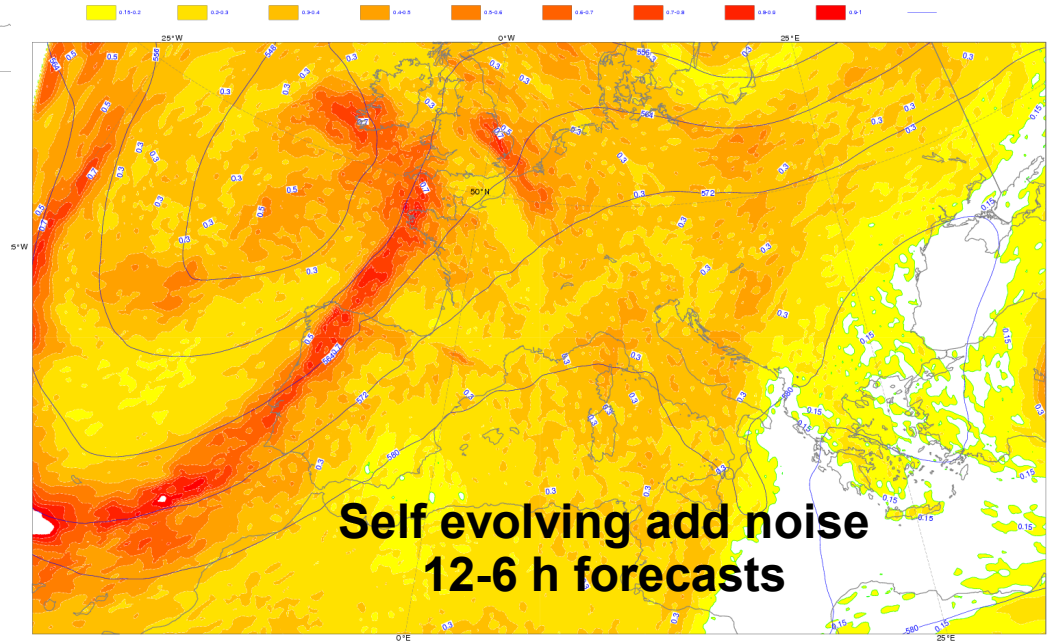




# Operational vs Self Evolv Additive Noise

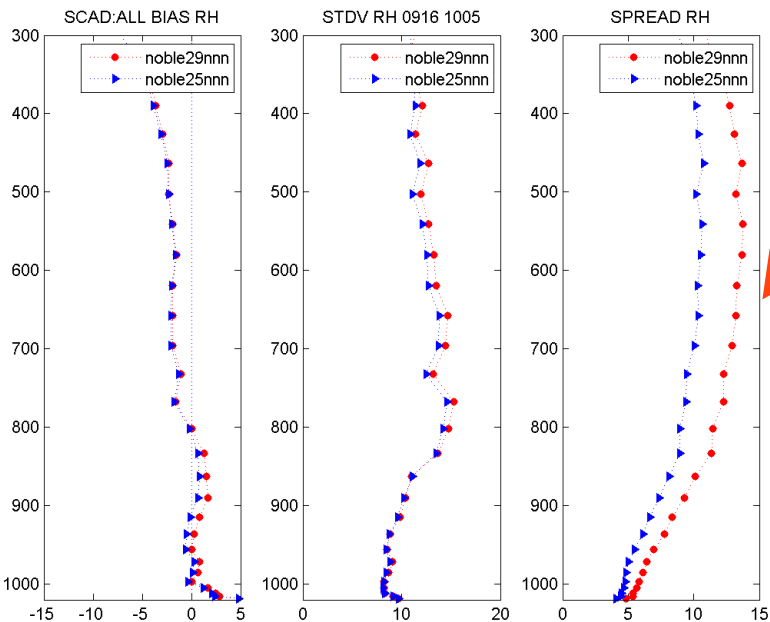
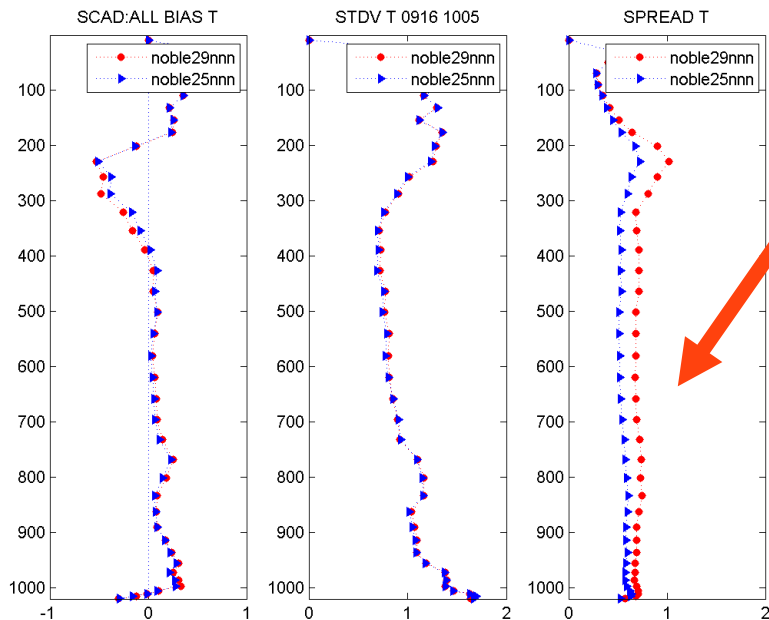
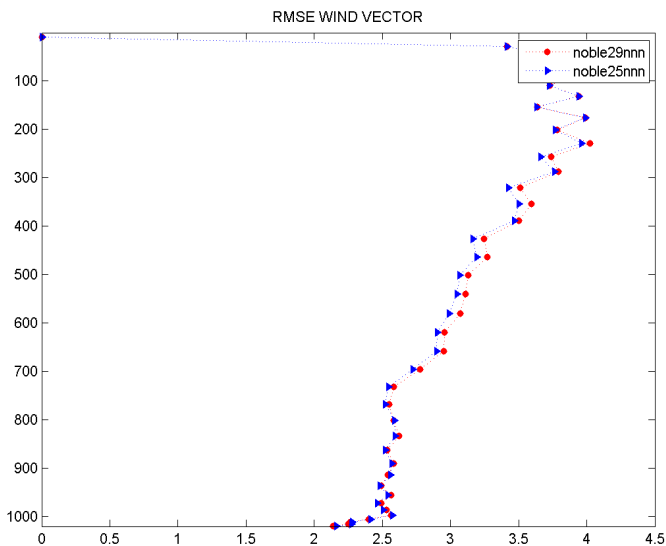


stdv add. T perturbation @ 500hPa





# Obs Increment Statistics



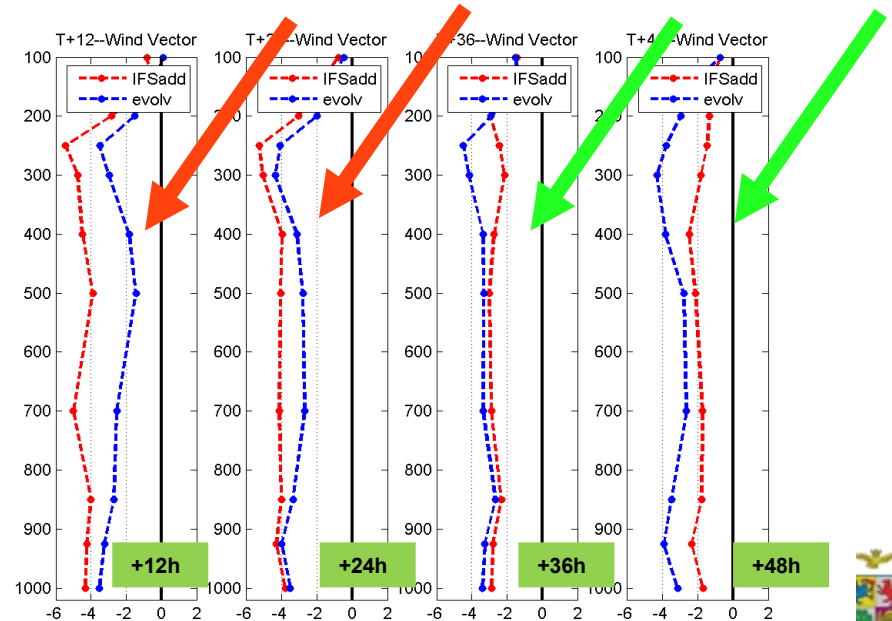
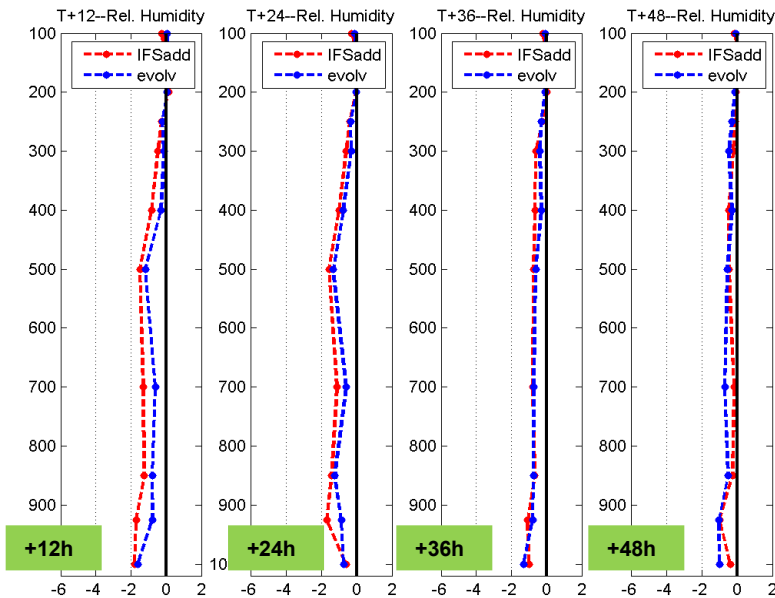
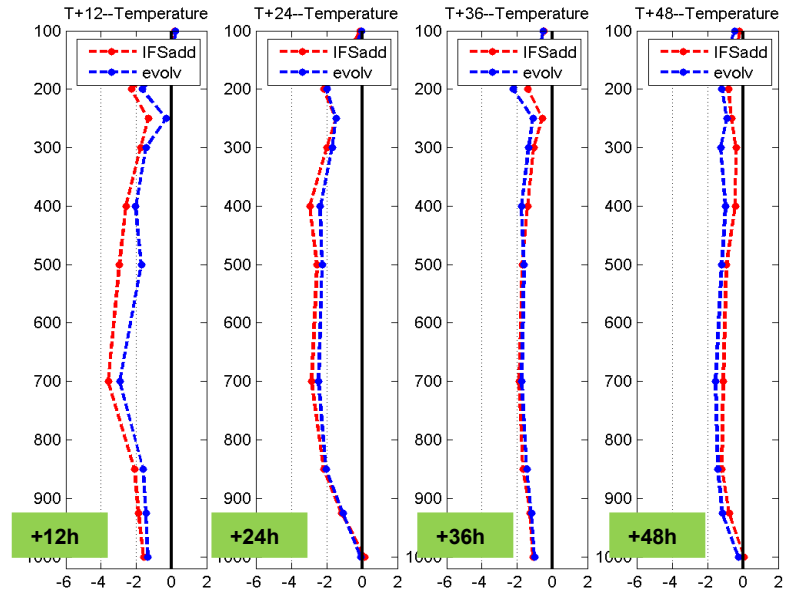
OBS INCREMENT ON **MODEL**  
 LEVELS (TEMP + RAOB obs)  
**IFS ADD** VS **EVOLVED 12-6h**  
 16 sept 2012 – 5 oct 2012





# Forecast Verification

Relative difference (%) in RMSE, computed against IFS analysis, with respect to **NO-ADDITIVE** run for 00 UTC COSMO runs from 16 sept 2012 – 5 oct 2012  
*negative value = positive impact*



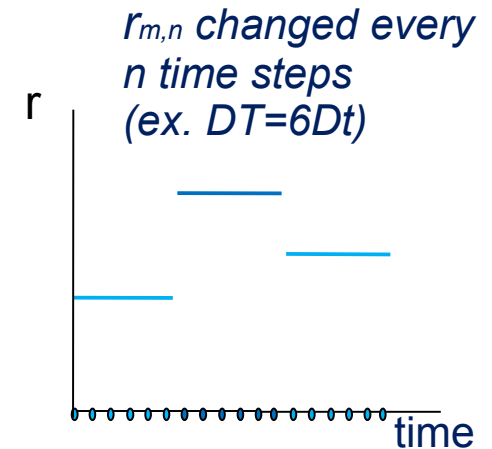
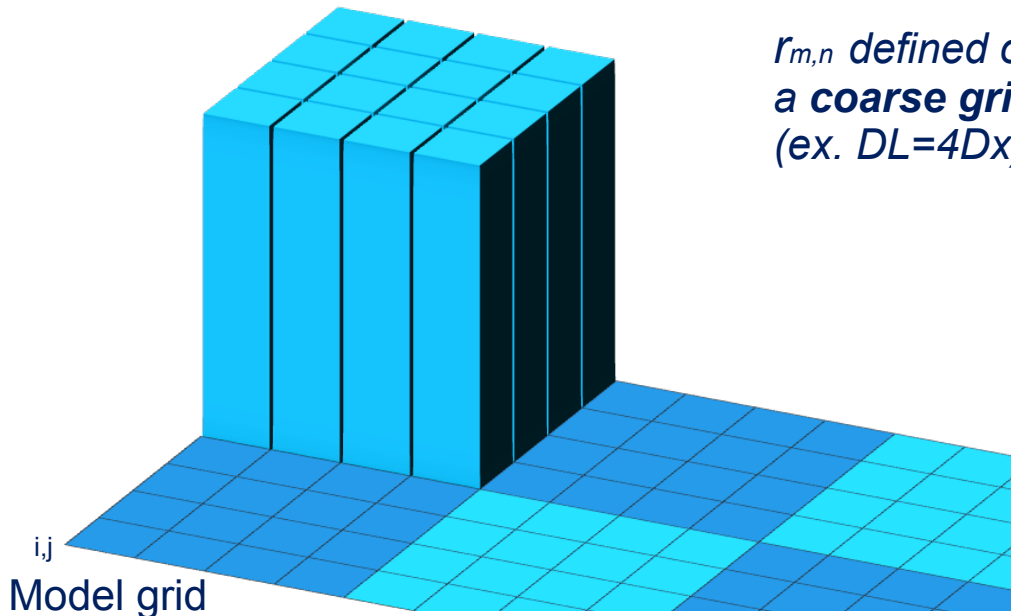


# Stochastic Perturbed Physics Tendency

- Model uncertainty could be represented also with a stochastic physics scheme (Buizza et al, 1999; Palmer et al, 2009) implemented in the prognostic model
- This scheme perturbs model physics tendencies by adding perturbations, which are proportional in amplitude to the unperturbed tendencies  $X_c$ :

$$X_p = (1 + r \mu) X_c$$

$r_{m,n}$  defined on a coarse grid (ex.  $DL = 4Dx$ )



## COSMO Version (by Lucio Torrisi)

Random numbers are drawn on a horizontal coarse grid from a Gaussian distribution with a stdv (0.1-0.5) bounded to a certain value (range =  $\pm 2-3$  stdv) and interpolated to the model grid to have a smoother pattern in time and horizontally in space. Same random pattern in the whole column and for  $u, v, t, qv$  variables.







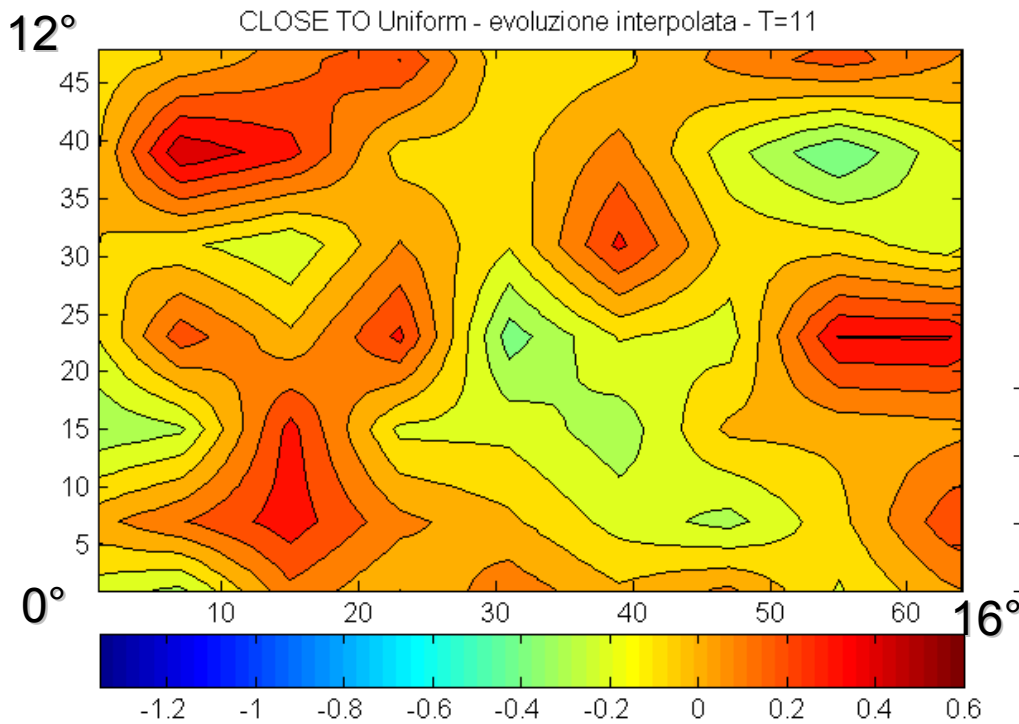
# Stochastic Physics

smoothed random pattern

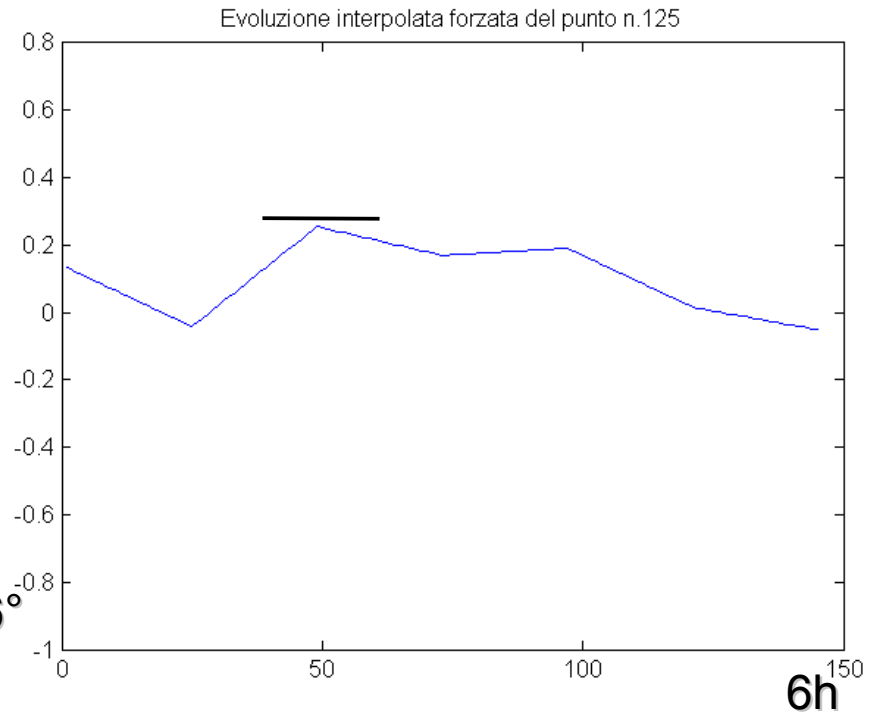
*Toy model and plots by A. Cheloni*

Model grid spacing:  $0.25^\circ$  (28 km)

Time step: 150 s



2.5° coarse grid with bilin. interp.



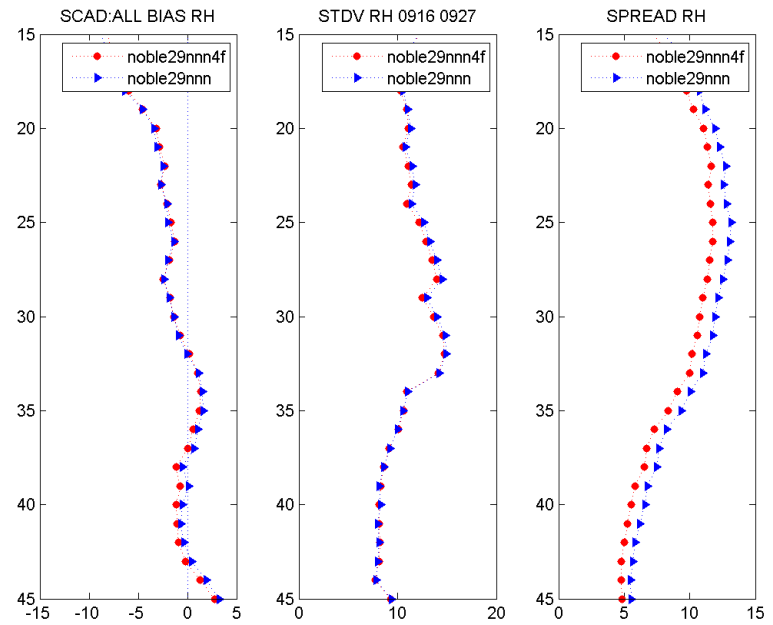
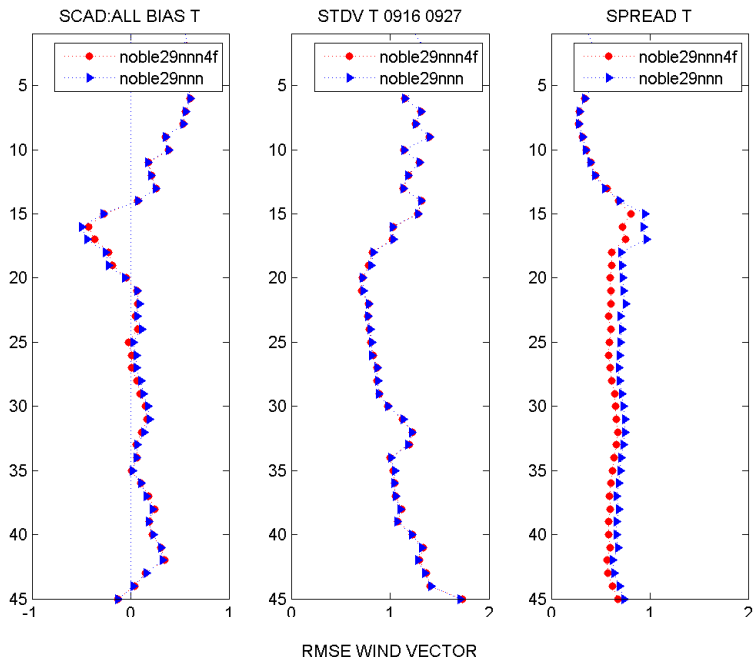
1h coarse time grid with lin. interp.





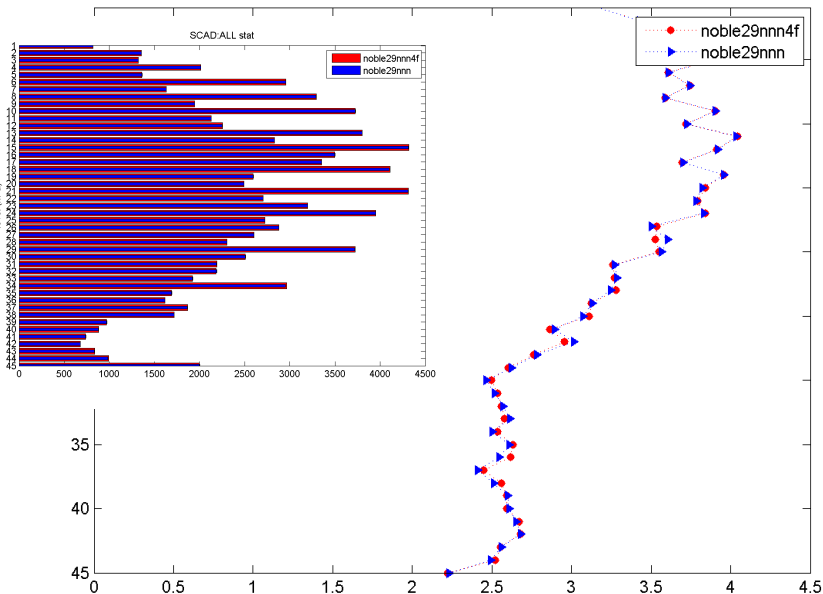
# OBS INCREMENT STATISTICS (RAOB)

## STOCHASTIC PHYSICS VS SELF-EVOLVING ADDITIVE



RMSE WIND VECTOR

**STOCHASTIC PHYSICS SETTINGS:**  
 stdv=0.25, range=0.5  
 box 2.5° x 2.5°, 3 hour  
 interp. in space and time  
 no humidity check



The impact on COSMO forecasts of SPPT seems to be smaller than those of additive noise (preliminar result)



# Summary and future steps

- “Self evolving additive noise” perturbations are both consistent with model errors statistics and a flow-dependent noise
- Additive noise computed using differences of forecasts with larger time distance (i.e. 18-6h) is computationally expensive and does not improve the scores as expected
- A better tuning of the 12-6 h forecast (filter and scaling factor) is planned
- A combination of self evolving additive noise and SPPT will be tested



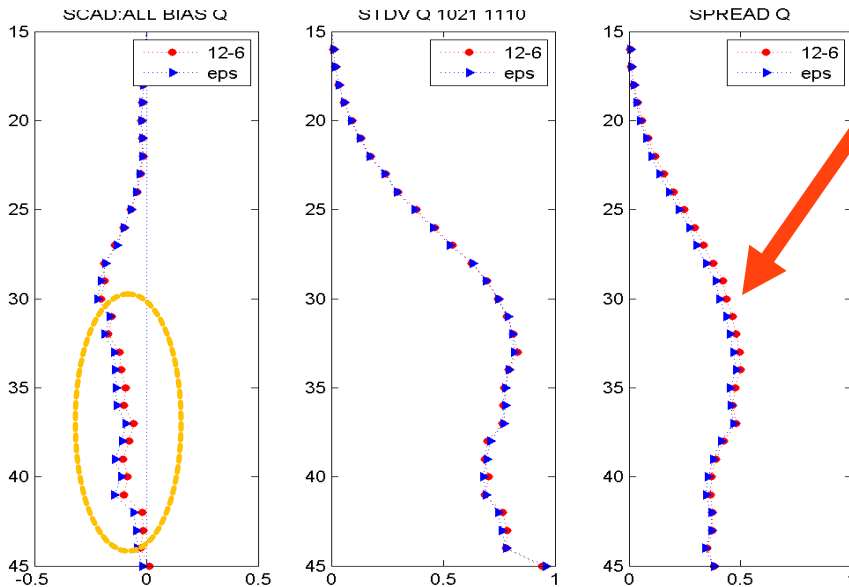
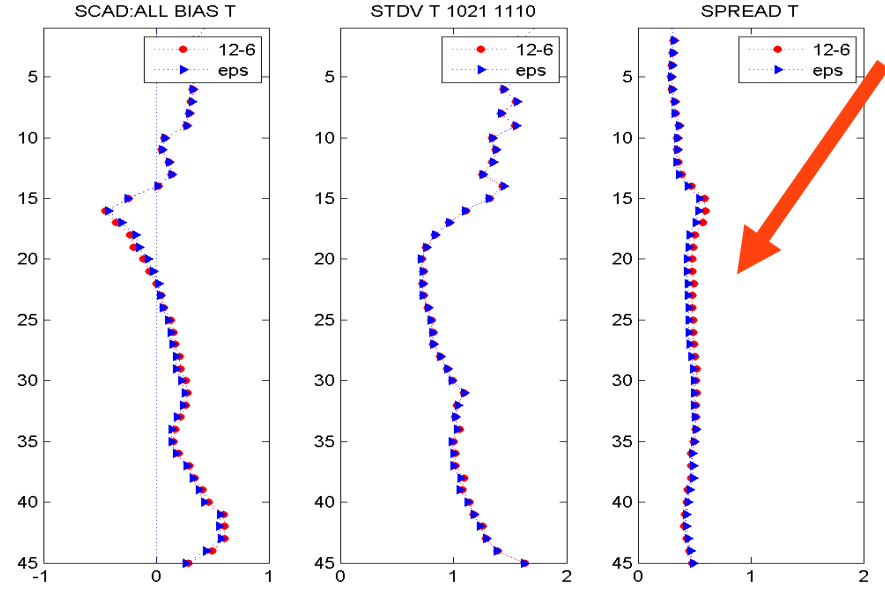
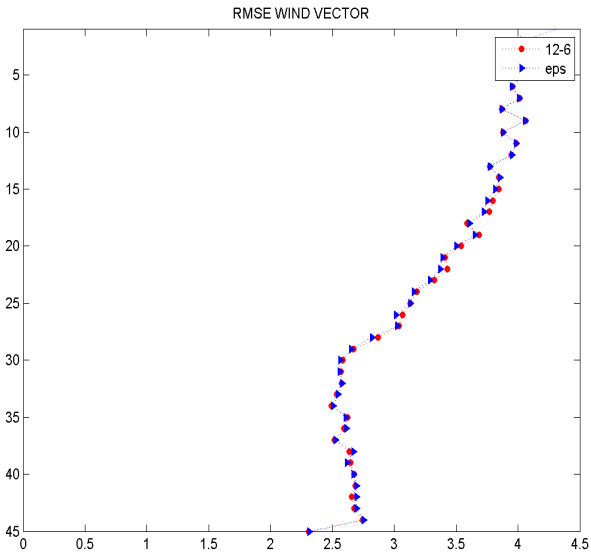


Thanks for your  
attention!





# Obs Increment Statistics



OBS INCREMENT ON **MODEL** LEVELS (TEMP + RAOB obs)  
**IFS ADD** VS **EVOLVED 12-6h**

21 oct 2013 – 10 nov 2013





# Forecast Verification

Relative difference (%) in RMSE, computed against IFS analysis, with respect to **NO-ADDITIVE** run for 00 UTC COSMO runs from 21 oct 2013 to 10 nov 2013  
*negative value = positive impact*

